

Ann Street School

Golf Team 2001



Sitting: from left to right: Alexei Yegorov, Christina Burgess, Ana Ferreira, Diogenes Lourenço
 Standing: from left to right: Rosalie Barbosa, Mario Fuentes, Ana Cristina Peña, Carlos Martins, Diane Castelo-Branco,
 Vice Principal Carmen E. Salgueiro, Teacher Manuel Oliveira, Vice Principal Jacquelyn Keene-Owens, Principal Joseph N. Maccia,
 Alexis Gonzalez, Daniel Barroqueiro, Jakub Wresilo, Jorge Abrantes, & Peter Brandao

Mathletics

Given the theme "Mathletics", our 8th grade class chose to find out how math permeates the game of golf.

We started out by researching golf courses for our study. When doing our research we found that the word Weequahic is a Lenni Lenape name which means boundary. Since Weequahic Park is in our own backyard and its name is associated with math, we decided to use it for our project. We contacted Mr. Joseph Lanzara from the Department of Parks at Essex County who faxed us a scale model of the park. We then drew a larger model using scale drawing where we incorporated ratios, proportions, conversion factors, and perimeters. Next we constructed a model of the golf course.

The second phase was to incorporate the topography of the park by creating a 3-D model representing land elevations. We did this by incorporating what we learned about slopes and plotting them on an X, Y grid.

The third phase was to illustrate the trajectory and distance of how far a ball can be hit. As we all know individual strength varies, therefore, we needed to create a scenario where both strength and speed would be near constant. We created a mechanical golfer, which works similar to a pendulum. We set the mechanical golfer into motion to find the velocity, angles and the loft of the clubs. We recorded the data and used it to solve for the trajectory path of the ball.

The fourth phase was to take a site visit to the United States Golf Association in Far Hills, NJ where we took a tour of their facility and interviewed Mr. John M. Spitzer Assistant Technical Director. He offered us the formulas needed to solve for the trajectory of the ball.

The final phase was to put our theory to practice. We visited Weequahic and conducted our field test research. Golf instructors, Mr. Ed Wadood, Mr. Nelson Tejada, and Mr. Donnell Redding assisted us with our golf stance, grip, and swing. We then had the opportunity to put our theory into practice and play a game of golf.



JAMES W. TREFFINGER
COUNTY EXECUTIVE

COUNTY OF ESSEX
DEPARTMENT OF PARKS, RECREATION AND CULTURAL AFFAIRS
115 CLIFTON AVENUE
NEWARK, NEW JERSEY 07104
TELEPHONE: 973-268-3500
FACSIMILE: 973-481-5302



DANIEL K. SALVANTE
DIRECTOR

FAX TRANSMITTAL

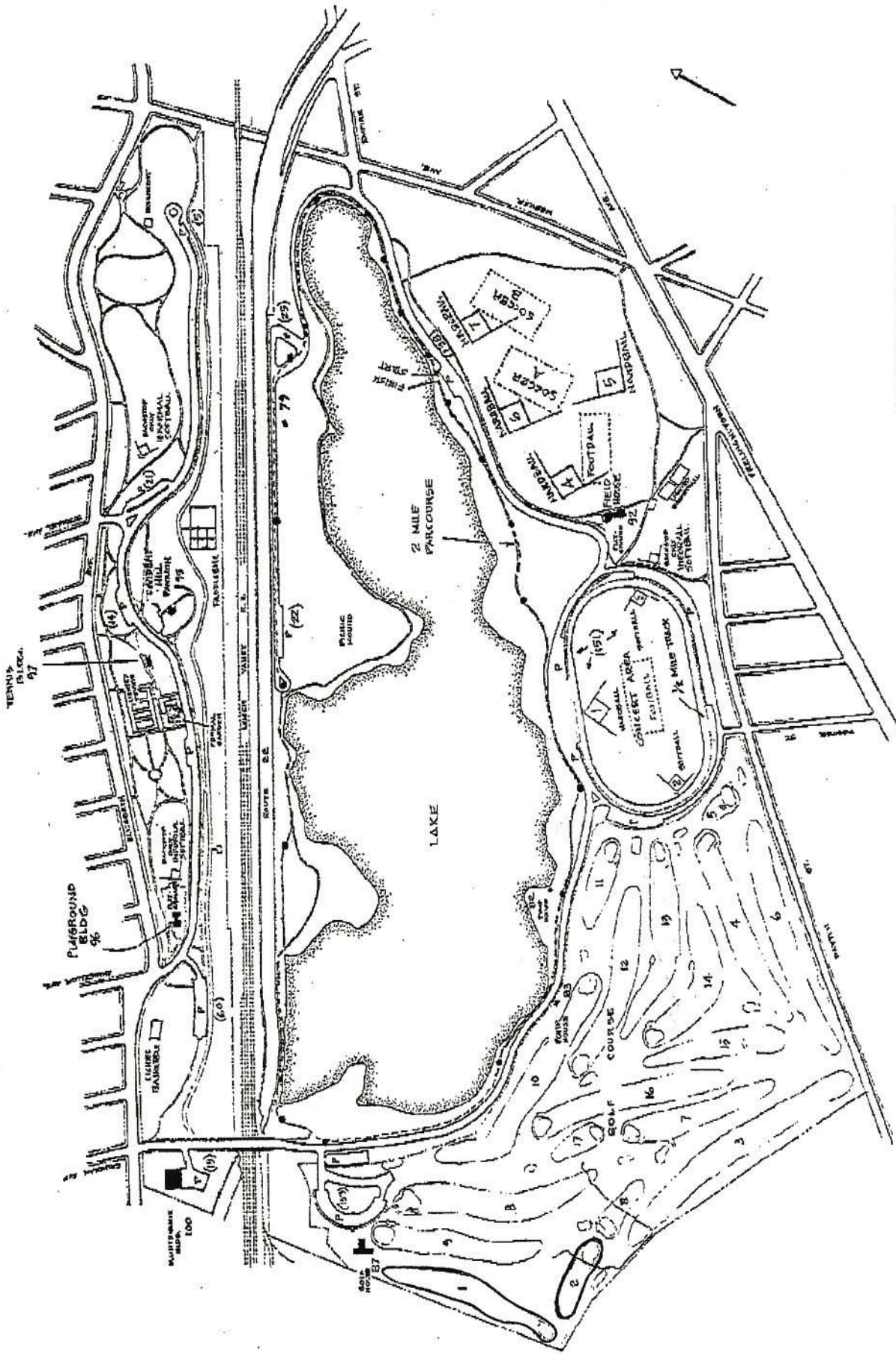
TO: FAX NUMBER 465-4185
NAME MANNY OLIVERA
LOCATION ANN ST. SCHOOL

FROM: JOSEPH LANZARA
PHONE: (973) 268-3500 Ext. 238
FAX: (973) 481-5302

DATE: 3-27-01

TOTAL NUMBER OF PAGES INCLUDING COVER LETTER 2

MESSAGE: WEEQUAHIC PARK - 311.33 ACRES (INCLUDING GOLF C.)
WEEQUAHIC GOLF COURSE - 69.90 ACRES
PLEASE CALL IF YOU NEED MORE
INFORMATION.



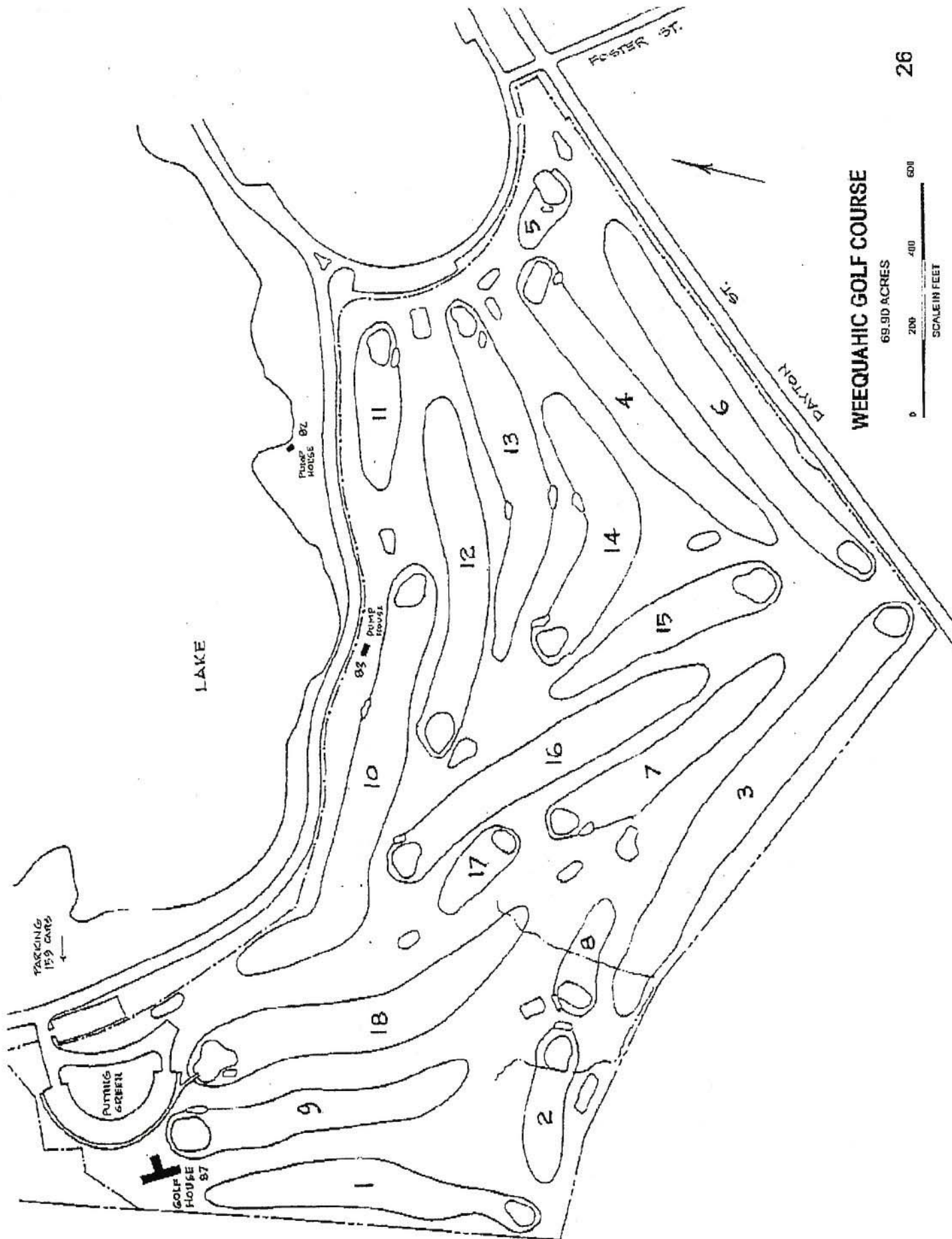
WEEQUAHIC PARK

311.33 ACRES



P = PARKING AREA
() = NO. OF SPACES

Golf course
69.90 acres



WEEQUAHIC GOLF COURSE

69.90 ACRES



Scale:

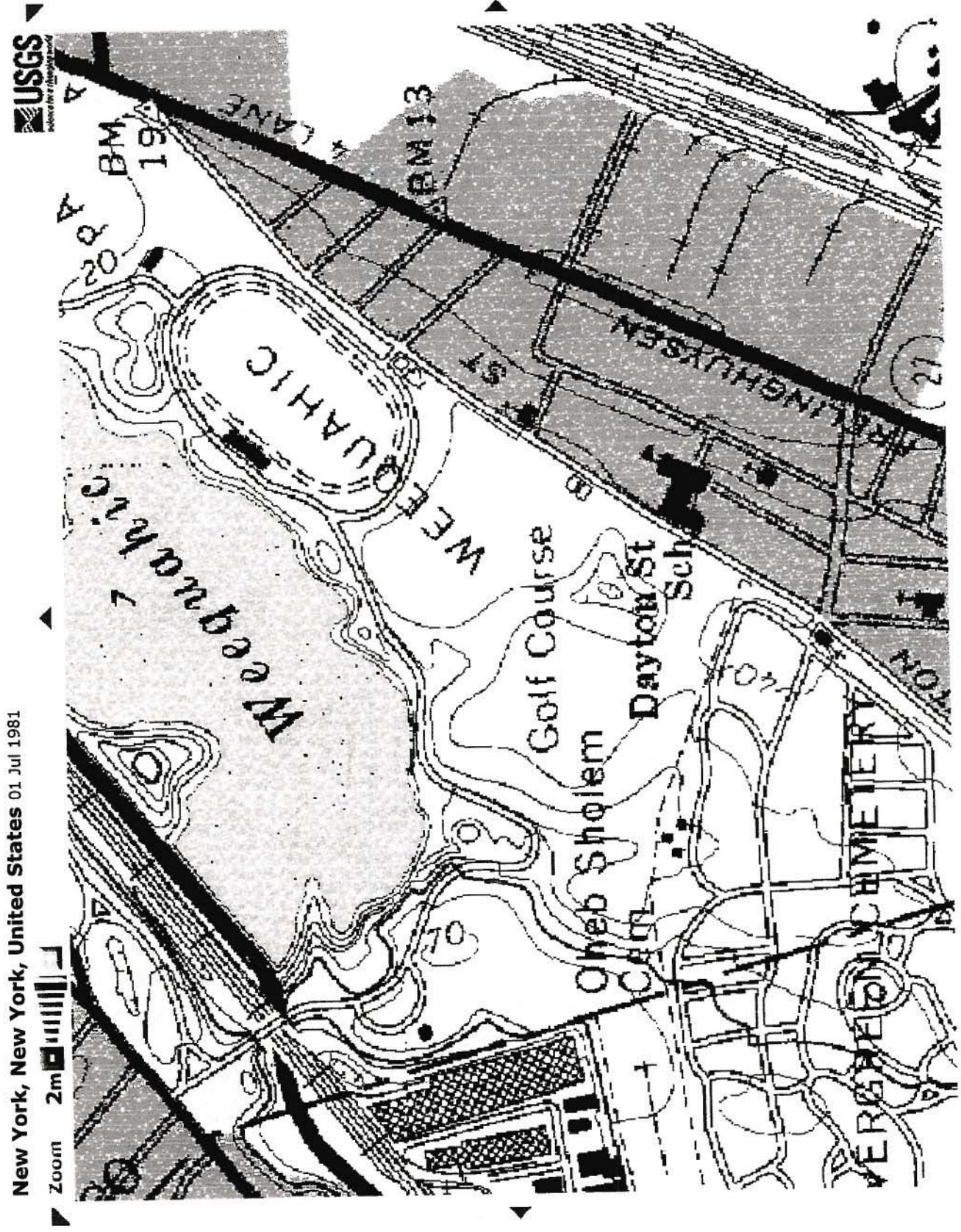
1 in. = 360 ft.

Mathletics

Hole #	Measurements in inches	Conversion Factor for feet	Total distance in feet	Conversion Factor for yards	Approx. Distance of the Hole
1	$2 \frac{11}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	967.5 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	322.5 yds.
2	1.25 in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	450 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	150 yds.
3	$4 \frac{1}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,462.5 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	487.5 yds.
4	$3 \frac{3}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,147 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	382.5 yds.
5	$\frac{14}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	315 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	105 yds.
6	4 in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,440 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	480 yds.
7	2.5 in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	900 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	300 yds.
8	$1 \frac{3}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	427.5 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	142.5 yds.
9	2.75 in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	990 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	330 yds.
10	$3 \frac{14}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,395 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	465 yds.
11	$1 \frac{7}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	517.5 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	172.5 yds.
12	$3 \frac{2}{16}$ in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,125 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	375 yds.

Mathletics

Hole #	Measurements in inches	Conversion Factor for feet	Total distance in feet	Conversion Factor for yards	Approx. Distance of the Hole
13	$3 \frac{6}{16} \text{ in.}$	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,215 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	405 yds.
14	2.75 in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	990 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	330 yds.
15	$2 \frac{1}{16} \text{ in.}$	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	742 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	247.5 yds.
16	$3 \frac{5}{16} \text{ in.}$	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,192.5 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	397.5 yds.
17	$1 \frac{1}{16} \text{ in.}$	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	382.5 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	127.5 yds.
18	3 in.	$\frac{360 \text{ ft.}}{1 \text{ in.}}$	1,080 ft.	$\frac{1 \text{ yd.}}{3 \text{ ft.}}$	360 yds.



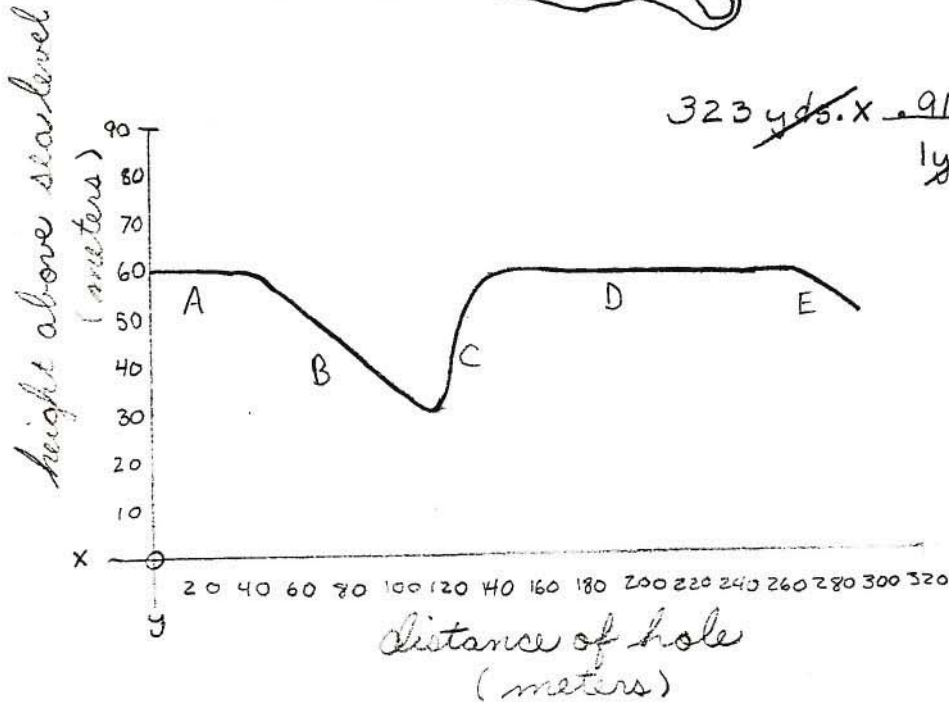
Weequahic Golf Course

Topography/Slope Hole



323 yds.

$$323 \text{ yds.} \times \frac{0.914 \text{ m}}{1 \text{ yd.}} \approx 295.2 \text{ m}$$



A- Slope = 0

B- Vertical Change = -30

Horizontal Change = 80

$$\text{Slope} = -\frac{30}{80} = -\frac{3}{8}$$

C- Vertical Change = 30

Horizontal Change = 20

$$\text{Slope} = \frac{30}{20} = \frac{3}{2} = 1\frac{1}{2}$$

D- Slope = 0

E- Vertical Change = -10

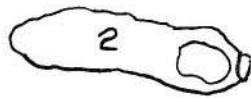
Horizontal Change = 30

$$\text{Slope} = -\frac{10}{30} = -\frac{1}{3}$$

Weequahic Golf Course

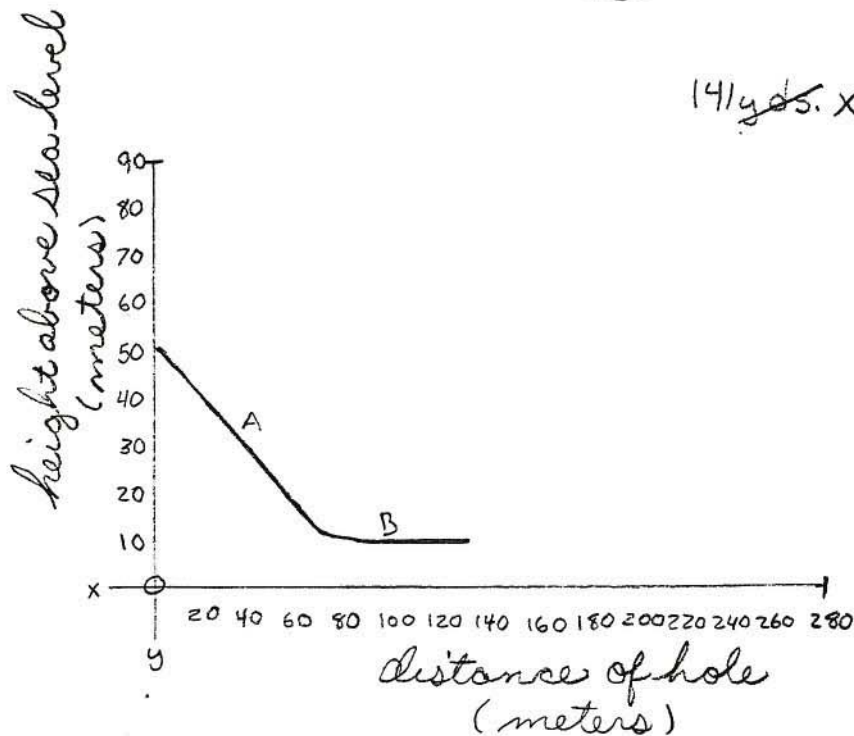
Topography/Slope

Hole



141 yds.

$$141 \text{ yds.} \times \frac{0.914 \text{ m}}{1 \text{ yd}} \approx 129 \text{ m.}$$



A = Vertical Change = -40

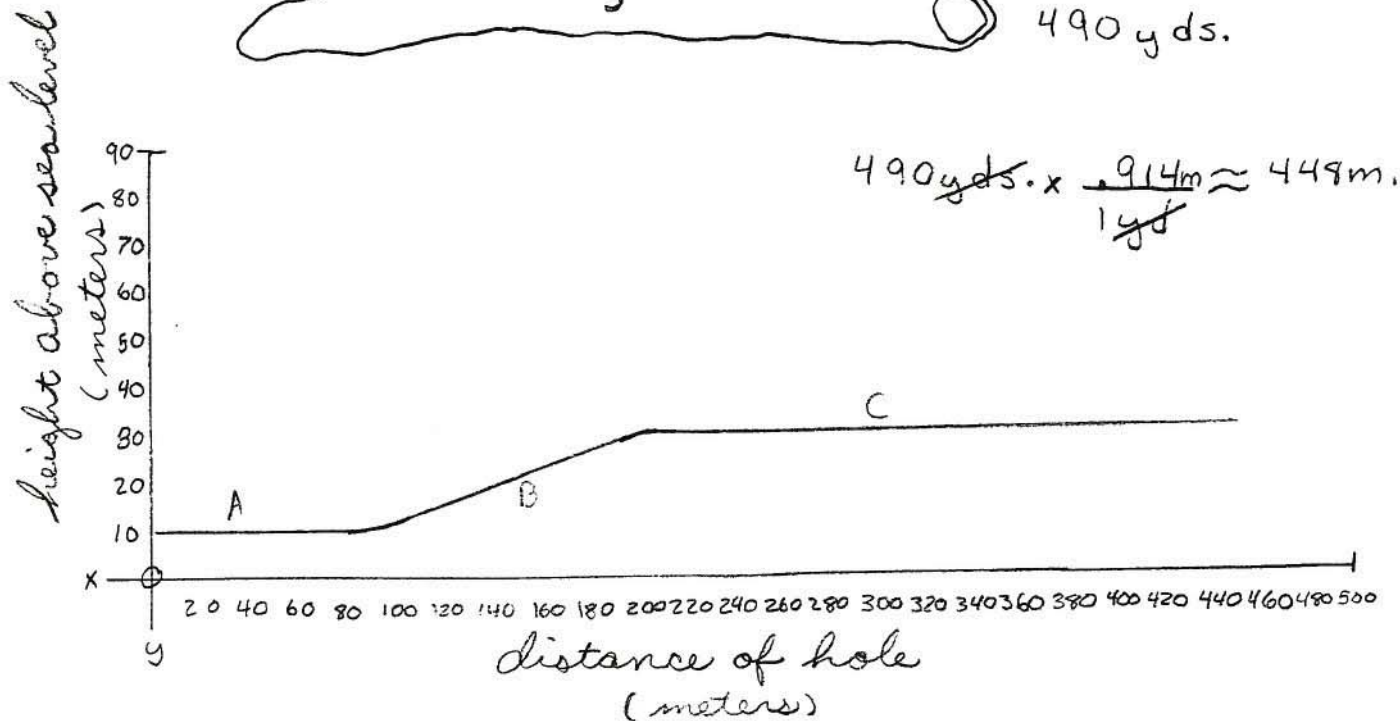
Horizontal Change = 70

Slope = $-\frac{40}{70} = -\frac{4}{7}$

B = Slope = 0

Weequahic Golf Course

Topography / Slope Hole



A- Slope = 0

B- Vertical Change = 20

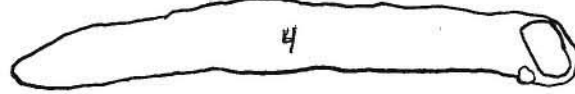
Horizontal Change = 100

$$\text{Slope} = \frac{20}{100} = \frac{2}{10} = \frac{1}{5}$$

C- Slope = 0

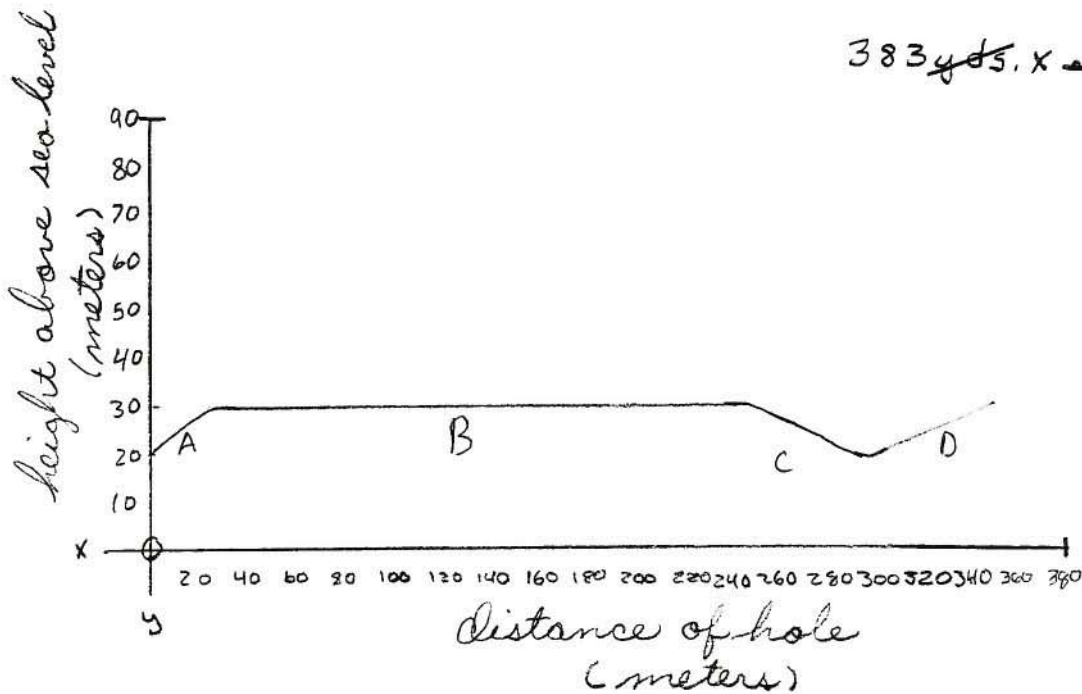
Weequahic Golf Course

Topography / Slope Hole



383 yds.

$$383 \text{ yds.} \times \frac{914 \text{ m}}{1 \text{ yd}} \approx 350 \text{ m.}$$



A- Vertical Change = 10
Horizontal Change = 20
Slope = $\frac{10}{20} = \frac{1}{2}$

D- Vertical Change = 10
Horizontal Change = 50
Slope = $\frac{10}{50} = \frac{1}{5}$

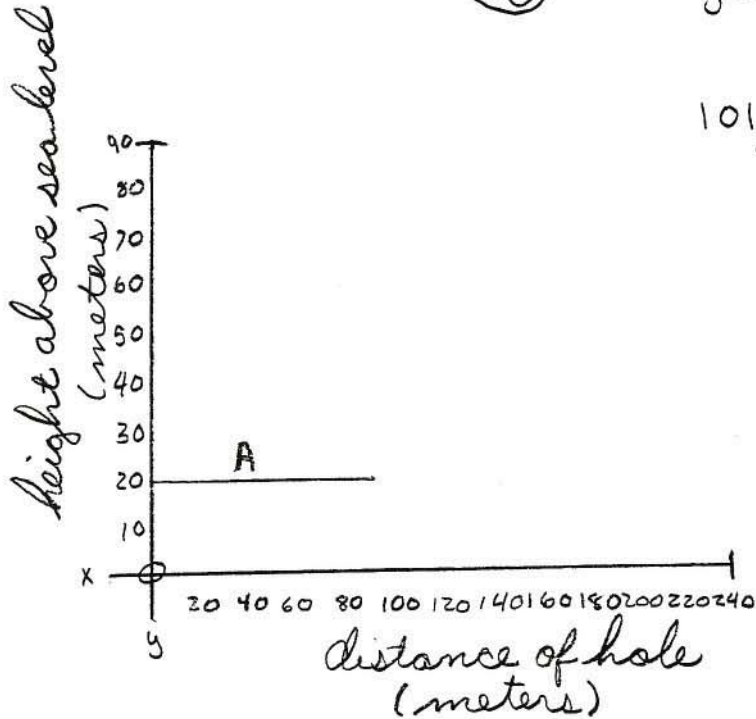
B- slope = 0

C- Vertical Change = -10
Horizontal Change = 50
Slope = $-\frac{10}{50} = -\frac{1}{5}$

Weequahic Golf Course

Topography / Slope Hole

5 101 yds.



$$101 \text{ yds.} \times \frac{.914 \text{ m}}{1 \text{ yd}} \approx 92.3 \text{ m.}$$

$$A - \text{Slope} = 0$$

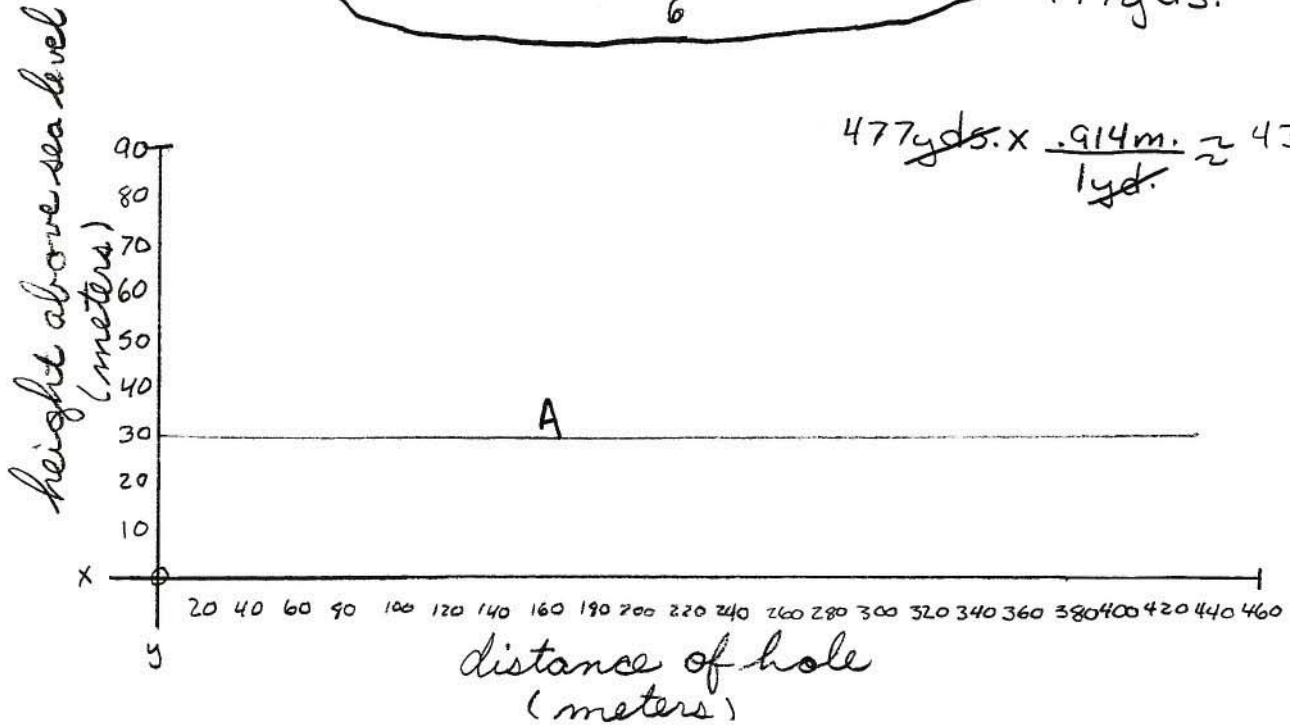
Weequahic Golf Course

Topography / Slope

Hole



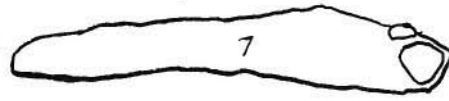
$$477 \text{ yds.} \times \frac{.914 \text{ m.}}{1 \text{ yd.}} \approx 436 \text{ m.}$$



A - Slope = 0

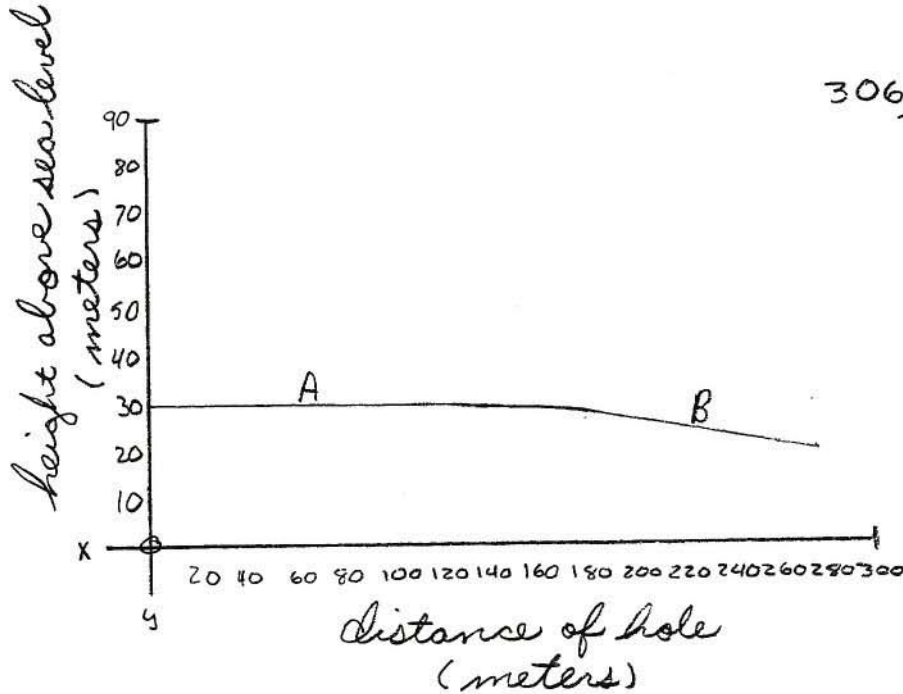
Weequahic Golf Course

Topography / Slope Hole



306 yds.

$$306 \text{ yds.} \times \frac{.914 \text{ m}}{1 \text{ yd.}} \approx 275 \text{ m.}$$



A - $\text{Slope} = 0$

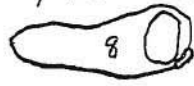
B - $\text{Vertical Change} = -10$

$\text{Horizontal Change} = 100$

$$\text{Slope} = \frac{-10}{100} = -\frac{1}{10}$$

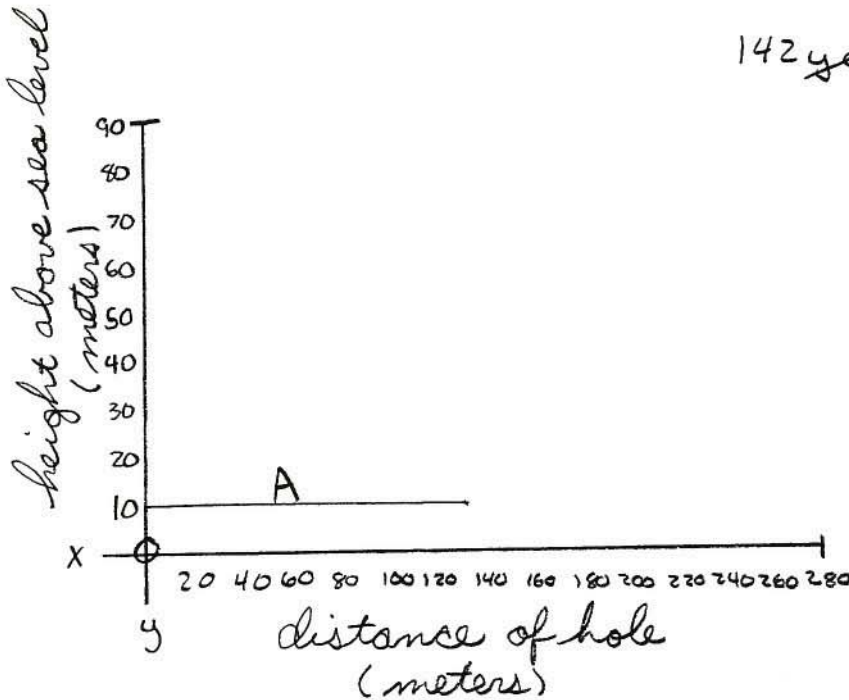
Weequahic Golf Course

Topography / Slope Hole



142 yds.

$$142 \text{ yds.} \times \frac{0.914 \text{ m}}{1 \text{ yd.}} \approx 130 \text{ m.}$$



A - Slope = 0

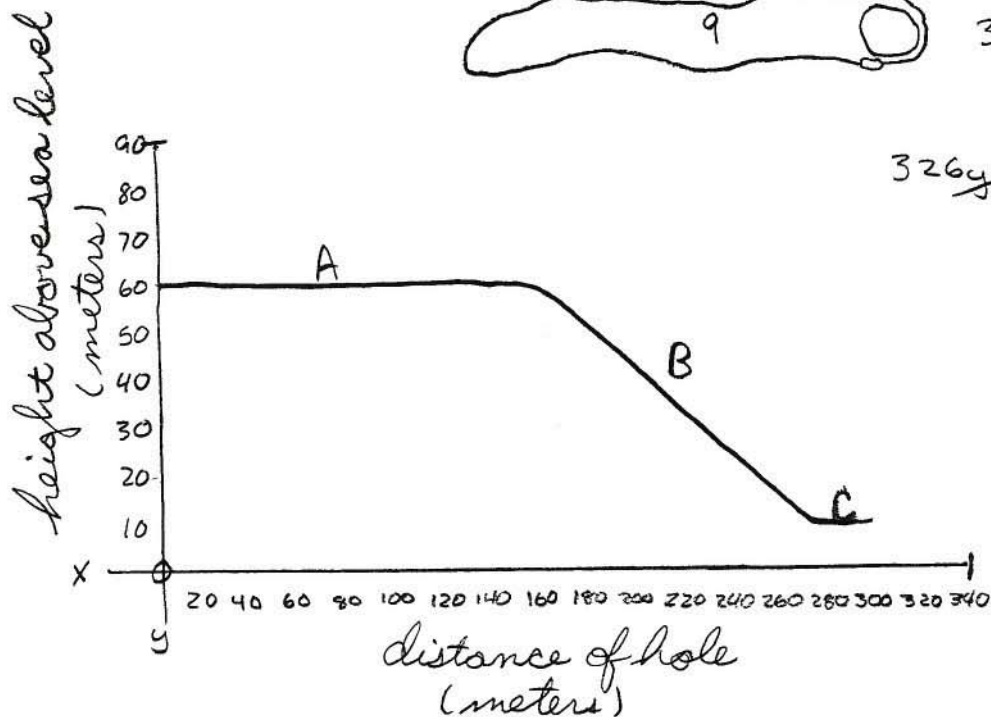
Weequahic Golf Course

Topography / Slope

Hole



$$326 \text{ yds.} \times \frac{.914 \text{ m}}{1 \text{ yd.}} \approx 298 \text{ m.}$$



$$A - \text{Slope} = 0$$

$$B - \text{Vertical Change} = -50$$

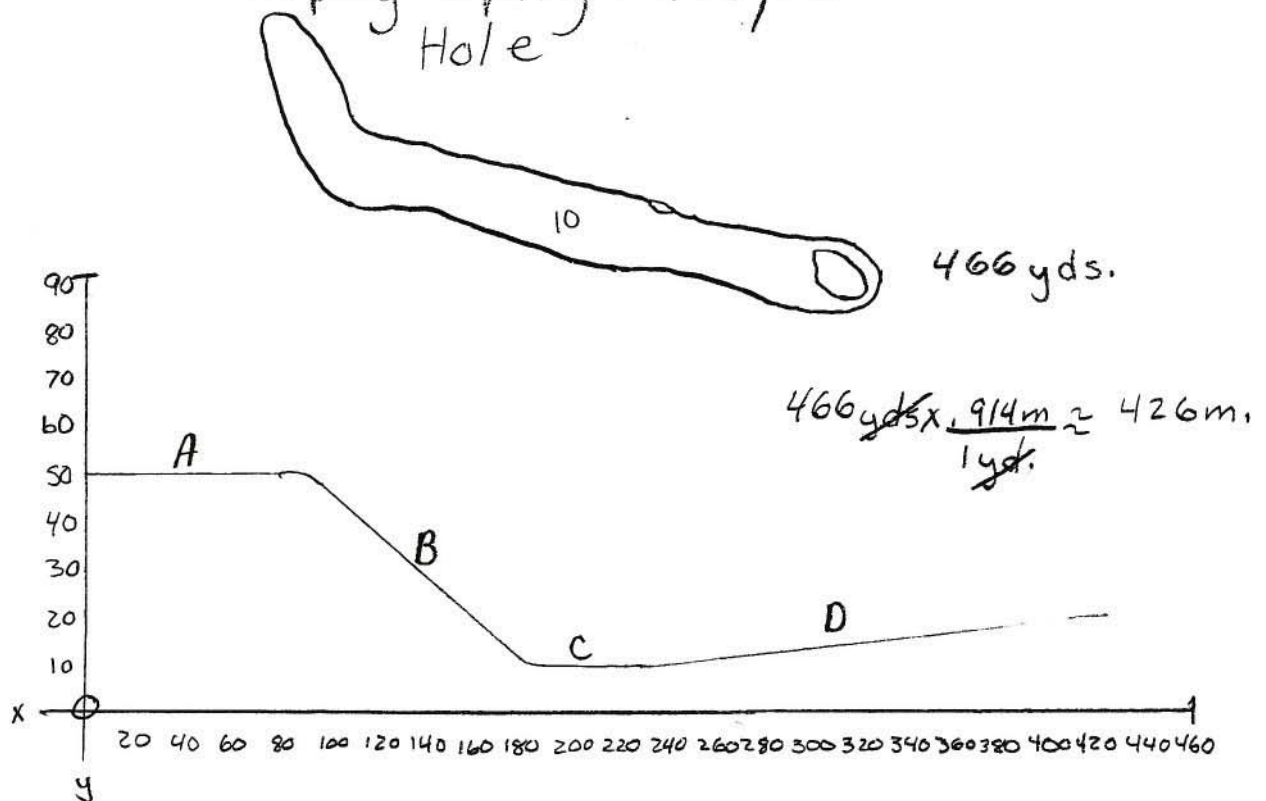
$$\text{Horizontal Change} = 110$$

$$\text{Slope} = -\frac{50}{110} = -\frac{5}{11}$$

$$C - \text{Slope} = 0$$

Weequahic Golf Course

Topography / Slope
Hole



A - Slope = 0

B - Vertical Change = -40

Horizontal Change = 80

Slope = $-\frac{40}{80} = -\frac{1}{2}$

C - Slope = 0

D. Vertical Change = 10

Horizontal Change = 200

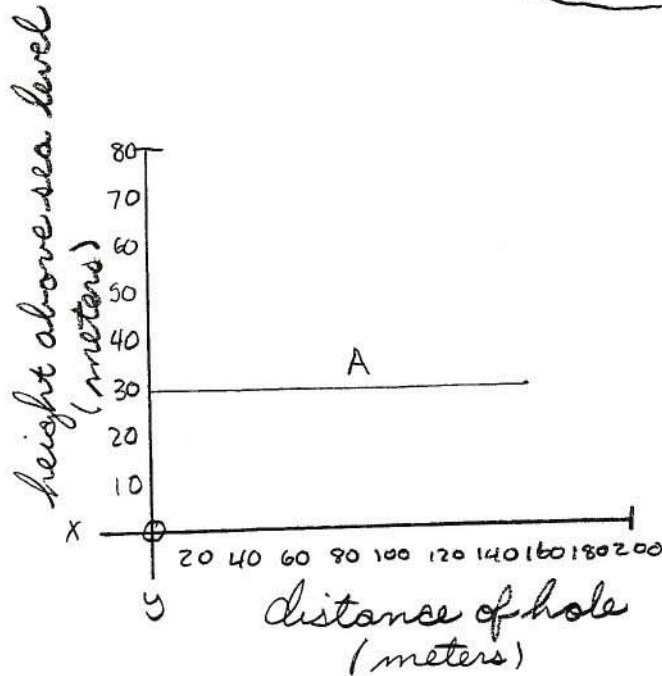
Slope = $\frac{10}{200} = \frac{1}{20}$

Weequahic Golf Course

Topography / Slope

Hole

11. 173 yds.

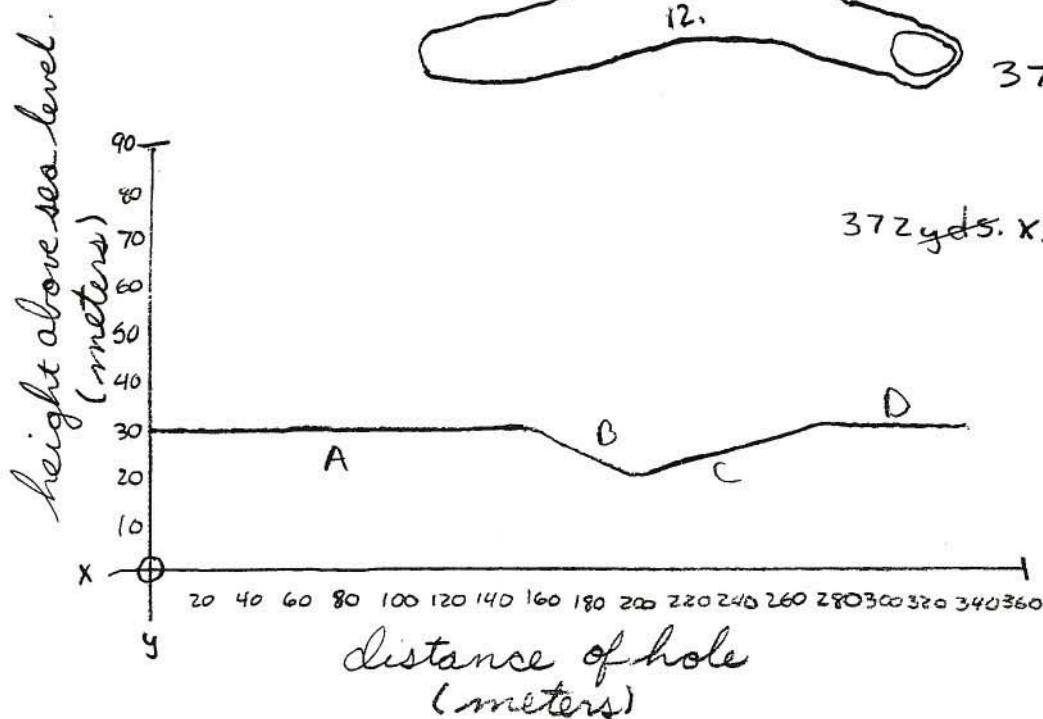


$$173 \text{ yds.} \times \frac{.914 \text{ m.}}{1 \text{ yd.}} \approx 158.1 \text{ m.}$$

A - slope = 0

Weequahic Golf Course

Topography / Slope Hole



A - Slope = 0

B - Vertical Change = -10

Horizontal Change = 40

$$\text{Slope} = \frac{-10}{40} = -\frac{1}{4}$$

C - Vertical Change = 10

Horizontal Change = 80

$$\text{Slope} = \frac{10}{80} = \frac{1}{8}$$

D - Slope = 0

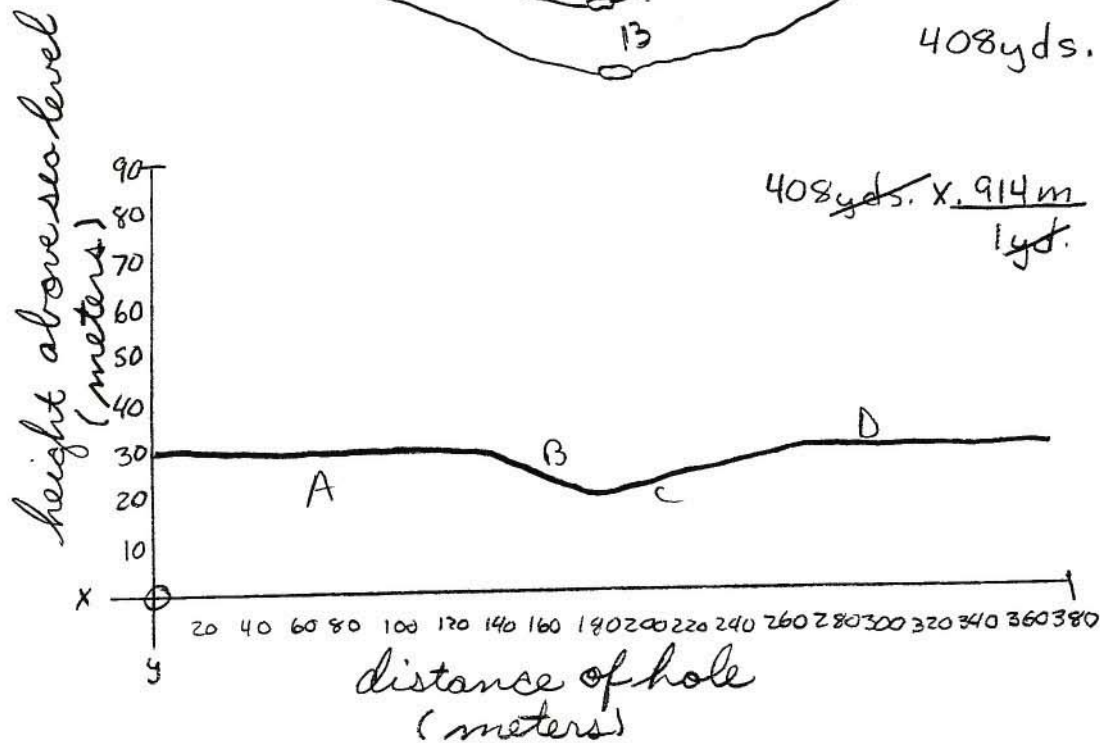
Weequahic Golf Course

Topography / Slope



408 yds.

$$408 \text{ yds.} \times \frac{0.914 \text{ m}}{1 \text{ yd.}} \approx 373 \text{ m.}$$



A - Slope = 0

B - Vertical Change = 10

Horizontal Change = 40

$$\text{Slope} = \frac{-10}{40} = -\frac{1}{4}$$

C - Vertical Change = 10

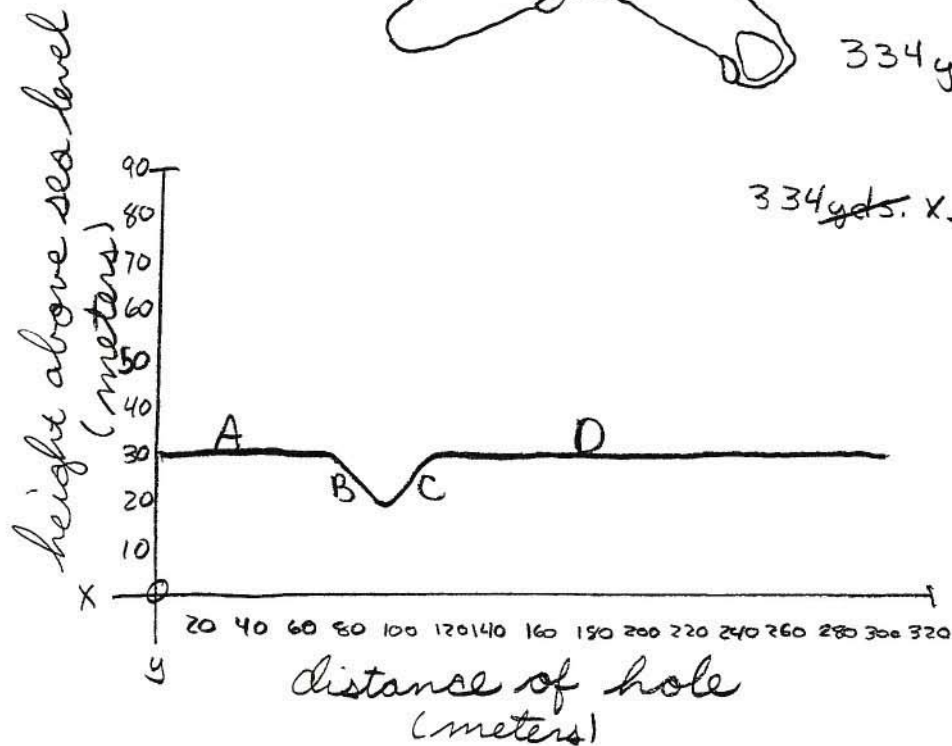
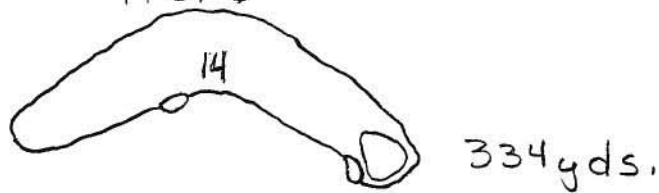
Horizontal Change = 80

$$\text{Slope} = \frac{10}{80} = \frac{1}{8}$$

D - Slope = 0

Weequahic Golf Course

Topography / Slope Hole



$$334 \text{ yds.} \times \frac{.914 \text{ m}}{1 \text{ yd}} \approx 305.3 \text{ m.}$$

A - Slope = 0

B - Vertical Change = -10

Horizontal Change = 20

$$\text{Slope} = \frac{-10}{20} = -\frac{1}{2}$$

C - Vertical Change = 10

Horizontal Change = 20

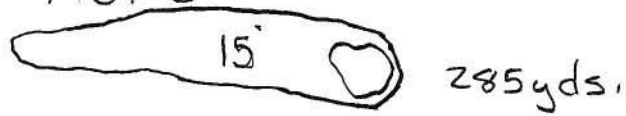
$$\text{Slope} = \frac{10}{20} = \frac{1}{2}$$

D - Slope = 0

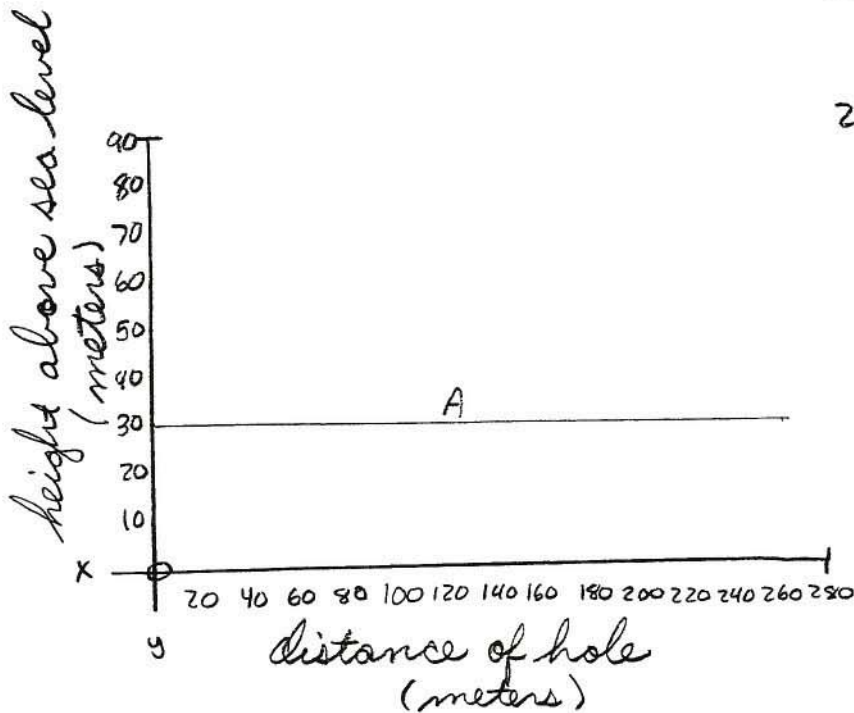
Weequahic Golf Course

Topography / Slope

Hole



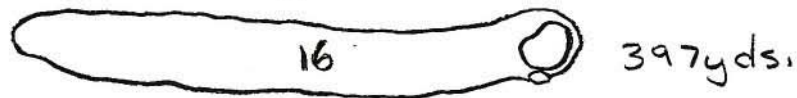
$$285 \text{ yds.} \times \frac{914 \text{ m}}{1 \text{ yd.}} \approx 261 \text{ m.}$$



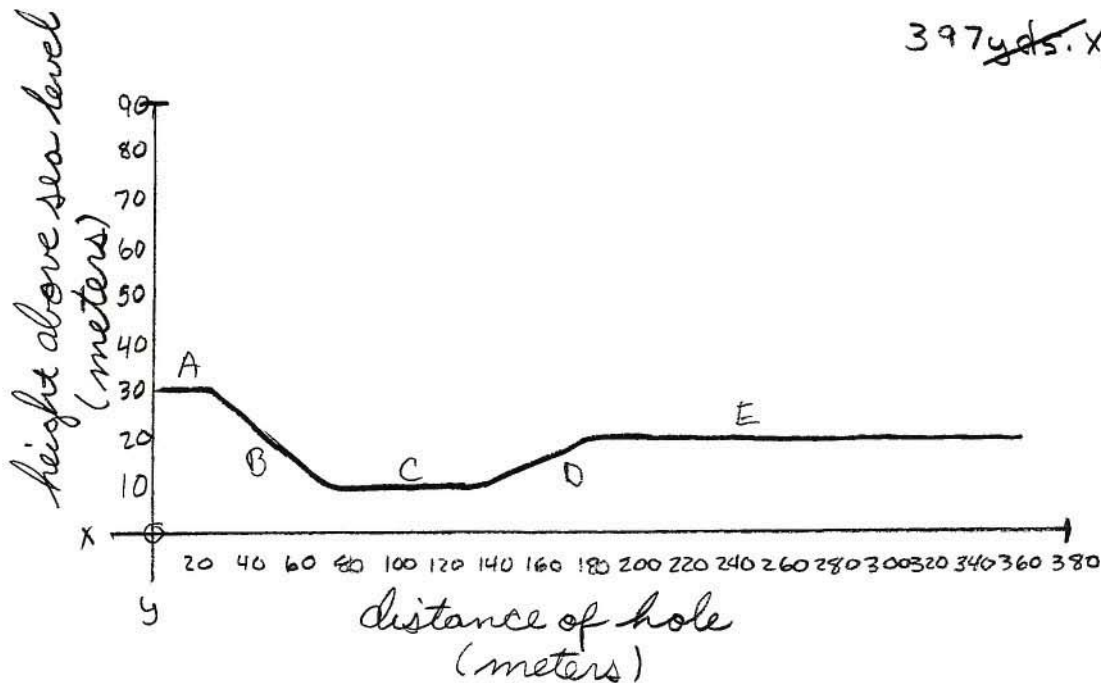
A - Slope = 0

Weequahic Golf Course

Topography / Slope Hole



$$397 \text{ yds.} \times \frac{0.914 \text{ m}}{1 \text{ yd.}} \approx 363 \text{ m.}$$



A- Slope = 0

B- Vertical Change = -20

Horizontal Change = 50

$$\text{Slope} = \frac{-20}{50} = -\frac{2}{5}$$

C- Slope = 0

D- Vertical Change = 10

Horizontal Change = 20

$$\text{Slope} = \frac{10}{20} = \frac{1}{2}$$

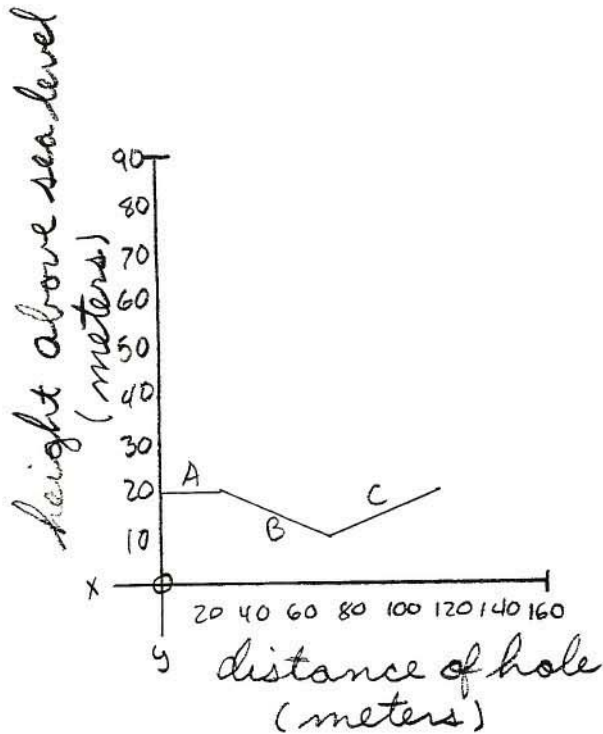
E- Slope = 0

Weequahic Golf Course

Topography / Slope

Hole

17 127yds.



$$127 \text{ yds.} \times \frac{0.914 \text{ m}}{1 \text{ yd}} \approx 116 \text{ m.}$$

A- Slope = 0

B- Vertical Change = -10

Horizontal Change = 40

$$\text{Slope} = \frac{-10}{40} = -\frac{1}{4}$$

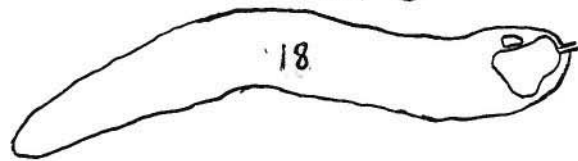
C- Vertical Change = 10

Horizontal Change = 40

$$\text{Slope} = \frac{10}{40} = \frac{1}{4}$$

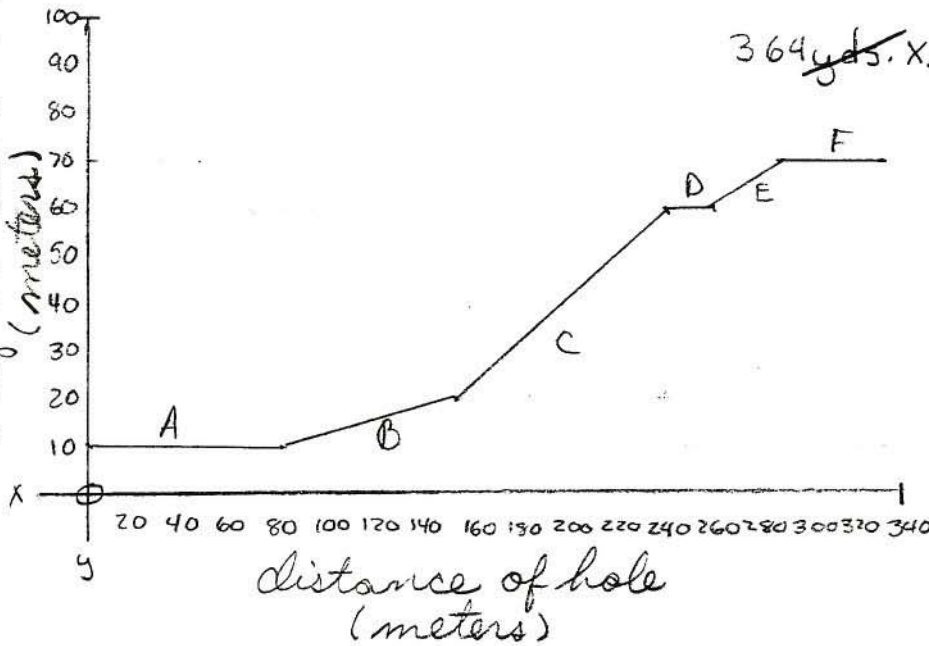
Weequahic Golf Course

Topography / Slope Hole



364 yds.

height above sea level
(meters)



$$364 \text{ yds.} \times \frac{.914 \text{ m}}{1 \text{ yd}} \approx 333 \text{ m.}$$

A- slope = 0

B- Vertical Change = 10

Horizontal Change = 70

$$\text{slope} = \frac{10}{70} = \frac{1}{7}$$

C- Vertical Change = 40

Horizontal Change = 90

$$\text{slope} = \frac{40}{90} = \frac{4}{9}$$

D- slope = 0

E- Vertical Change = 10

Horizontal Change = 20

$$\text{slope} = \frac{10}{20} = \frac{1}{2}$$

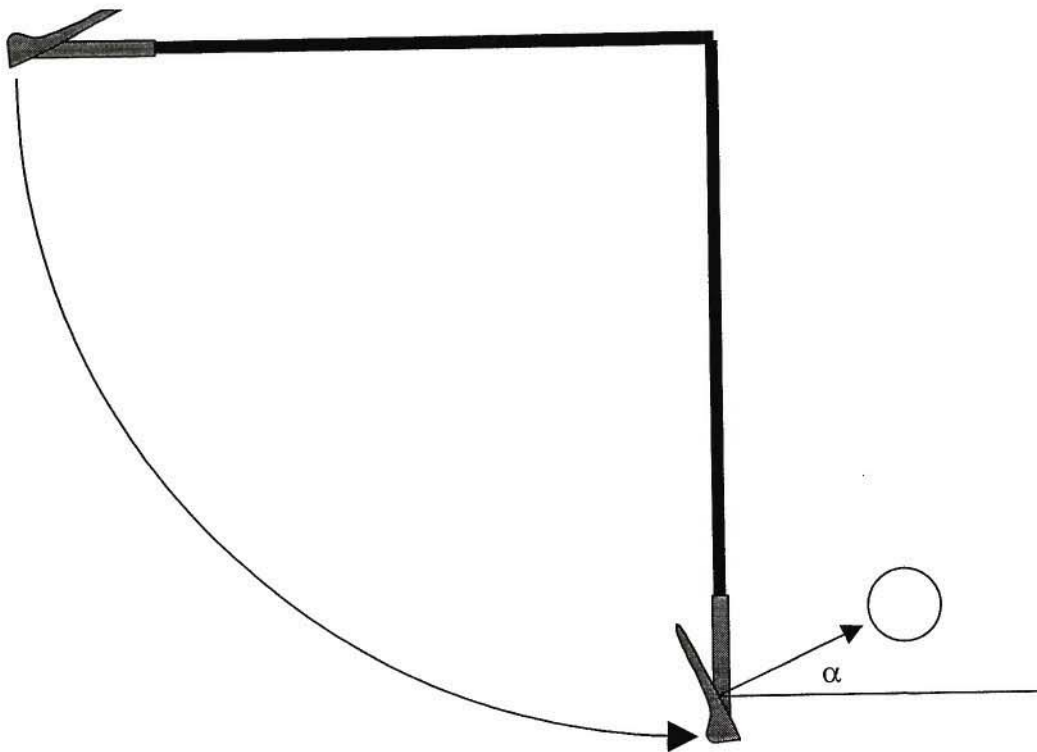
F- slope = 0

From: John Spitzer <JSpitzer@USGA.org> | [Block Address](#) | [Add to Address Book](#)
To: "'Oliveira401@yahoo.com"' <Oliveira401@yahoo.com>
Subject: Ann Street exp.doc
Date: Wed, 2 May 2001 10:47:23 -0400

Manny,

It was nice meeting you and your students the other day. Attached is a document with some basic equations. They include some simplifying assumptions that make them not exactly correct but they probably are not unreasonable for the grade level. Call if you have questions.

Good luck!
John



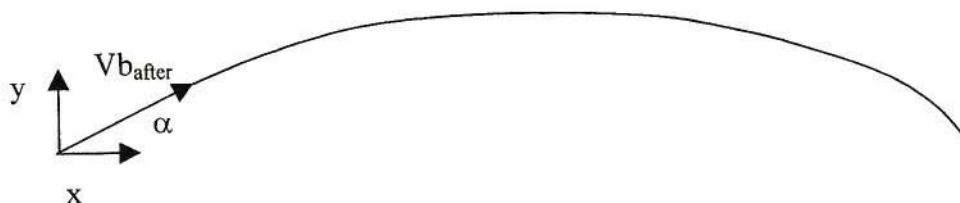
In your experiment you've released the club from 90° and timed how long it takes until impact. Knowing the time and distance traveled (calculated from the club length and the arc it makes with your "Wooden Byron) you can estimate an impact velocity, V_i .

The ball will leave the lofted club as some angle, α . That portion of V_i that propels the ball could be calculated as $V_i \cos(\alpha)$.

This is a little tricky but we could estimate the ball's velocity using the following formula, provided we know the mass of the ball M_b , and the mass of the clubhead, M_c (if you tell me the brand I can probably get that info for you so you don't have to take the shaft out of the club) and assume the ball has a coefficient of restitution, e , of 0.85 (which is not unreasonable)

$$V_{b_{\text{after}}} = (M_c V_i (1+e)) / (M_c + M_b) \quad [1]$$

If we then use the equations of motion we can estimate a distance from the initial launch (neglecting any aerodynamic effects)



The initial velocity of the ball in the y direction is:

$$V_{by0} = V_{b\text{after}} \sin(\alpha) \quad [2]$$

Gravity pulls the ball down so the velocity of the ball in the y direction at any time is:

$$V_{by} = V_{by0} + a \cdot t \text{ where } a \text{ is the acceleration of gravity and } t \text{ is time.}$$

We can find the position in y using the following equation:

$$y = V_{by0} \cdot t + \frac{1}{2} a \cdot t^2 \quad [3]$$

Eventually the vertical velocity upwards goes to zero and the ball begins to fall to the ground. The acceleration of the ball in the y direction at any time is:

$$V_{by}^2 = (V_{by0})^2 + a \cdot y \quad [4]$$

where a is the acceleration of gravity and t is time.

The horizontal direction is given by:

$$V_{bx0} = V_{b\text{after}} \cos(\alpha) \quad [5]$$

We can find the position in x using the following equation (gravity doesn't act in this direction):

$$x = V_{bx0} \cdot t \quad [6]$$

and the maximum height by using equation [4] with $V_{by}^2 = 0$.

You measured the time, distance and maximum height. When you calculate x using [6] and the measured time does it agree with the distance measured? (probably not) When you calculate the maximum height, y, using [4] does it agree with your measurement? (Again probably not) This is OK because you neglected aerodynamics and estimated the velocity. Next year you can add these features.

Mathletics

Distance (in inches) ~ Time (in seconds) that the ball traveled.

Ball: Top Flight ~ Weight: 46 grams

Pitching Wedge- 45°

	D	T
1)	30 ~	.31
2)	33 ~	.36
3)	32 ~	.35
4)	36 ~	.39
5)	32 ~	.34

D	T
38 ~	.41
31 ~	.33
37 ~	.40
35 ~	.38
36 ~	.39

Avg. distance the ball traveled: 34 inches in .37 seconds

9 iron- 41°

1)	38 ~	.37
2)	46 ~	.41
3)	41 ~	.39
4)	43 ~	.39
5)	50 ~	.43

34 ~	.35
46 ~	.42
38 ~	.36
44 ~	.40
40 ~	.38

Avg. distance the ball traveled: 42 inches in .39 seconds

8 iron- 37°

1)	45 ~	.40
2)	50 ~	.43
3)	36 ~	.40
4)	54 ~	.44
5)	42 ~	.39

47 ~	.42
47 ~	.42
47 ~	.42
45 ~	.40
41 ~	.38

Avg. distance the ball traveled: 45 inches in .41 seconds

7 iron- 34°

1)	44 ~	.36
2)	48 ~	.37
3)	48 ~	.37
4)	45 ~	.37
5)	48 ~	.40

48 ~	.41
50 ~	.41
48 ~	.38
51 ~	.41
52 ~	.42

Avg. distance the ball traveled: 48 inches in .39 seconds

Mathletics

6 iron- 31°

	D	T
1)	55	~ .38
2)	40	~ .36
3)	38	~ .35
4)	60	~ .40
5)	53	~ .38

D	T
62	~ .41
47	~ .38
42	~ .37
58	~ .39
45	~ .38

Avg. distance the ball traveled: 50 inches in .38 seconds

5 iron- 28°

1)	36	~ .30
2)	40	~ .32
3)	42	~ .33
4)	40	~ .32

38	~ .32
46	~ .35
42	~ .33
52	~ .40

Avg. distance the ball traveled: 44 inches in .35 seconds

4 iron- 25°

1)	46	~ .30
2)	50	~ .32
3)	48	~ .31
4)	51	~ .33
5)	51	~ .33

56	~ .36
52	~ .35
55	~ .35
58	~ .37
60	~ .38

Avg. distance the ball traveled: 53 inches in .34 seconds

3 iron- 22°

1)	36	~ .26
2)	37	~ .28
3)	40	~ .32
4)	38	~ .31
5)	39	~ .31

39	~ .30
38	~ .30
37	~ .27
38	~ .29
39	~ .30

Avg. distance the ball traveled: 38 inches in .29 seconds

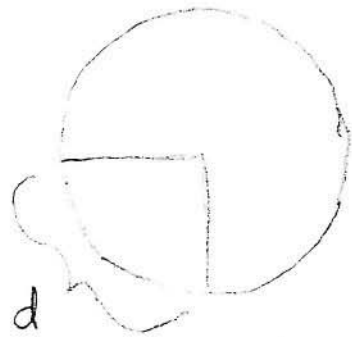
Pitching wedge

Angle is 45°

Club Length is 36 in. = .914 m.

Mass of Ball is 46 g (M_b)

Mass of the clubhead is 280 g (M_c)



Circumference = $2\pi r$

Distance = $\frac{1}{4}(2\pi r) = \frac{1}{4}(2)(3.14)(36 \text{ in}) = 56.52 = 1.44 \text{ m}$

Time = .55 s (T)

Acceleration of Gravity = 9.8 m/s^2

Time ball is in flight from initial launch to landing + varying from .01 s to .37 s

At maximum time of .37 s the ball traveled in x direction:
34 in = .86 m

Calculations

Impact Velocity (V_i) = $d/t = 1.44 \text{ m} / .55 \text{ s} = 2.62 \text{ m/s} = 5.86 \text{ mph}$

Partial V_i is the portion of V_i that propels the ball

$V_i \cos(45^\circ) = 2.62 \text{ m/s} (.707) = 1.85 \text{ m/s} = 4.14 \text{ mph}$

① Velocity of the ball after impact

$V_{\text{after}} = (M_c V_i \cos(\theta)) / (M_c + M_b)$

$V_{\text{after}} = [280 \text{ g} (1.85 \text{ m/s}) (.707)] / (280 \text{ g} + 46 \text{ g}) = 2.94 \text{ m/s} = 6.58 \text{ mph}$

② Initial Velocity of the ball in the y direction

$V_{by0} = V_{\text{after}} \sin(\alpha) = 2.94 \text{ m/s} (.707) = 2.08 \text{ m/s} = 4.65 \text{ mph}$

③ Find position of y using the following equation

$y = V_{by0} t + \frac{1}{2} a t^2$

$y = 2.08 \text{ m/s} (t) + \frac{1}{2} (-9.8 \text{ m/s}^2) (t^2)$

for $t = .01 \text{ s}$ $y = .02 \text{ m} = .79 \text{ in}$

for $t = .37 \text{ s}$ $y = .09 \text{ m} = 3.54 \text{ in}$

④ The acceleration of the ball in the y direction at any time

is $V_{by}^2 = (V_{by0})^2 + a y$

to get the maximum height, $V_{by}^2 = 0$

$y = (-V_{by0}^2) / a = (-2.08 \text{ m/s})^2 / (-9.8 \text{ m/s}^2) = .44 \text{ m} = 17.32 \text{ in}$

⑤ $V_{bx0} = V_{\text{after}} \cos(\alpha) = 2.94 \text{ m/s} (.707) = 2.08 \text{ m/s} = 4.65 \text{ mph}$

⑥ Since gravity does not act in this direction, the following equation will give us the position of x

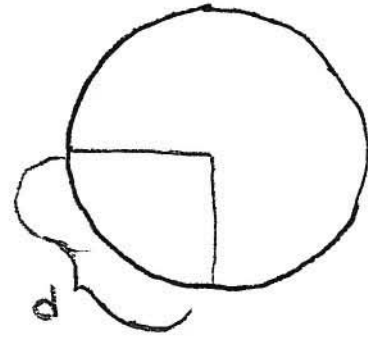
$$x = v_b x_0 * t = 2.08 \text{ m/s}(t)$$

$$\text{for } t = .01 \text{ s } \quad x = .02 \text{ m} = .79 \text{ in}$$

$$\text{for } t = 0.37 \text{ s } \quad x = .77 \text{ m} = 30.31 \text{ in.}$$

9 Iron

angle: 41°
 club length: $36\text{ in} = .914\text{ m}$
 mass of ball: $(M_b) = 46\text{ g}$
 mass of club head: $(M_c) = 280\text{ g}$



$$\text{Circumference} = 2\pi r$$

Distance

$$d = \frac{1}{4}(2\pi r) = \frac{1}{4}(2)(3.14)(36\text{ in}) = 56.52\text{ in} = 1.44\text{ m}$$

Time

$$t = .55\text{ s}$$

Acceleration of gravity
 $a = 9.8\text{ m/s}^2$

Time ball is in flight from initial launch to landing
 t varying from $.01\text{ s}$ to 0.47 s

At maximum time of $.47\text{ s}$ the ball traveled in x direction = $42\text{ in} = 1.07\text{ m}$

Calculations

$$\text{Impact velocity } V_i = d/t = 1.44\text{ m} / .55\text{ s} = 2.62\text{ m/s} = 5.86\text{ mph}$$

Partial V_i is the portion of V_i that propels the ball

$$V_i^* = V_i (\cos 41^\circ) = 2.62\text{ m/s} (.755) = 1.96\text{ m/s} = 4.38\text{ mph}$$

(1) Velocity of the ball after impact

$$V_{\text{after}} = (M_c V_i^* (1+e)) / (M_c + M_b)$$

$$V_{\text{after}} = [280\text{ g} (1.96\text{ m/s}) (1+0.85)] / (280\text{ g} + 46\text{ g}) = 3.11\text{ m/s} = 6.91\text{ mph}$$

(2) Initial Velocity of the ball in the y direction

$$V_{by0} = V_{\text{after}} \sin(\alpha) = 3.11\text{ m/s} (.656) = 2.04\text{ m/s} = 4.56\text{ mph}$$

(3) Position of $y =$

$$y = V_{by0} t + \frac{1}{2} a t^2$$

$$y = 2.04\text{ m/s}(t) + \frac{1}{2}(-9.8\text{ m/s}^2)(t^2)$$

$$\text{for } t = .01\text{ s } y = .02\text{ m} = .79\text{ in}$$

$$\text{for } t = .39\text{ s } y = .04\text{ m} = 1.57\text{ in}$$

(4) Acceleration of the ball in the y direction is

$$V_{by}^2 = (V_{by0})^2 + a y$$

$$\text{maximum height } t = V_{by}^2 = 0$$

$$y = (-V_{by0}^2) / a = (-2.04\text{ m/s})^2 / (-9.8\text{ m/s}^2) = .42\text{ m} = 16.54\text{ in}$$

(5) Horizontal direction

$$V_{bx0} = V_{\text{after}} \cos(\alpha) = 3.11\text{ m/s} (.755) = 2.35\text{ m/s} = 5.26\text{ mph}$$

(6) Since gravity does not act in this direction, the following equation will give us the position of x

$$x = v_{bx0} * t = 2.35 \text{ m/s} (t)$$

$$\text{for } t = .015 \text{ s } x = .02 \text{ m} = .79 \text{ in}$$

$$\text{for } t = .395 \text{ s } x = .92 \text{ m} = 36.22 \text{ in}$$

8 IRON

Angle: 37°

Club Length: $36.25 \text{ in} = .921 \text{ m}$

Mass of Ball: 46 g

Mass of Club head: 280 g

Circumference = $2\pi R$

Distance

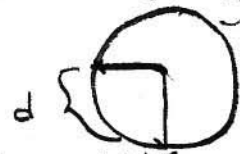
$$\frac{d}{\text{Time}} = \frac{1}{4} (2\pi R) = \frac{1}{4} (2) (3.14) (36.25 \text{ in}) = 56.91 \text{ in} = 1.45 \text{ m}$$

Time

$$t = .55 \text{ s}$$

Acceleration of Gravity

$$a = 9.8 \text{ m/s}^2$$



Time ball is in flight from initial launch to landing
+ varying from .01s to .41s

At maximum time of .41s the ball traveled in x direction =
 $45 \text{ in} = 1.14 \text{ m}$

Calculations

Impact velocity $V_i = d/t = 1.45 \text{ m} / .55 \text{ s} = 2.64 \text{ m/s} = 5.91 \text{ mph}$

Partial V_i is the portion of V_i that propels the ball

$$V_i^* = V_i (\cos 37^\circ) = 2.64 \text{ m/s} (.799) = 2.11 \text{ m/s} = 4.72 \text{ mph}$$

(1) Velocity of the ball after impact

$$V_{b \text{ after}} = (m_c V_i^* (1+e)) / (m_c + m_b)$$

$$V_{b \text{ after}} = [280 \text{ g} (2.11 \text{ m/s}) (1+0.85)] / (280 \text{ g} + 46 \text{ g}) = 3.35 \text{ m/s} = 7.49 \text{ mph}$$

(2) Initial Velocity of the ball in the y direction

$$V_{b y_0} = V_{b \text{ after}} \sin(\alpha) = 3.35 \text{ m/s} (.602) = 2.02 \text{ m/s} = 4.52 \text{ mph}$$

(3) Find position of y using the following equation

$$y = V_{b y_0} t + \frac{1}{2} a t^2$$

$$y = 2.02 \text{ m/s} (t) + \frac{1}{2} (-9.8 \text{ m/s}^2) (t^2)$$

$$\text{for } t = .01 \text{ s } y = .02 \text{ m} = .79 \text{ in}$$

$$\text{for } t = .41 \text{ s } y = .054 \text{ m} = .16 \text{ in}$$

(4) The acceleration of the ball in the y direction at any time:

$$V_{b y}^2 = (V_{b y_0})^2 + a y$$

to get to the maximum height, $V_{b y}^2 = 0$

$$y = (-V_{by0}^2) / a = (-2.02 \text{ m/s})^2 / (-9.8 \text{ m/s}^2) = .42 \text{ m} = 16.54 \text{ in}$$

(5) Horizontal direction is

$$V_{bx0} = V_{\text{after}} * \cos(\alpha) = 3.35 \text{ m/s} (.799) = 2.68 \text{ m/s} = 5.99 \text{ mph}$$

(6) Since gravity does not act in this direction, the following equation will give us the position of x

$$x = V_{bx0} * t = 2.68 \text{ m/s}(t)$$

$$\text{for } t = .01 \text{ s} \quad x = .03 \text{ m} = 1.18 \text{ in}$$

$$\text{for } t = .41 \text{ s} \quad x = 1.09 \text{ m} = 42.91 \text{ in}$$

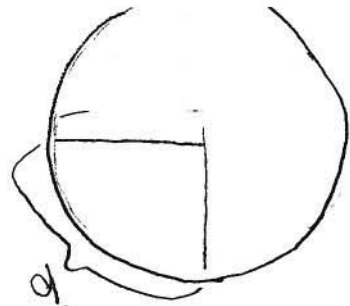
7 IRON

$$\text{Angle} = 34^\circ$$

$$\text{Club Length} = 36.75 \text{ in} = .933 \text{ m}$$

$$\text{mass of ball (} m_b \text{)} = 46 \text{ g}$$

$$\text{Mass of the club head (} m_c \text{)} = 280 \text{ g}$$



$$\text{Circumference} = 2\pi R$$

$$\text{Distance; } d = \frac{1}{4}(2\pi R) = \frac{1}{4}(2)(3.14)(36.75 \text{ in}) = 57.70 \text{ in} = 1.47 \text{ m}$$

$$\text{Time; } t = .55 \text{ s}$$

$$\text{Acceleration of gravity}$$

$$a = 9.8 \text{ m/s}^2$$

Time ball is in flight from initial launch to Landing
 t varying from .01s to .39s

At maximum time of .39s the ball traveled in x
 direction = 48 in = 1.22 m

Calculations

$$\text{Impact velocity } V_i = d/t = 1.47 \text{ m} / .55 \text{ s} = 2.67 \text{ m/s} = 5.97 \text{ mph}$$

Partial V_i is the portion of V_i that propels the ball
 $V_i^* = V_i (\cos 34^\circ) = 2.67 \text{ m/s} (.829) = 2.21 \text{ m/s} = 4.94 \text{ mph}$

1. Velocity of ball after impact

$$V_{\text{after}} = (m_c V_i^* (1+e)) / (m_c + m_b)$$

$$V_{\text{after}} = [280 \text{ g} (2.21 \text{ m/s}) (1+0.85)] / (280 \text{ g} + 46 \text{ g}) = 3.51 \text{ m/s} = 7.85 \text{ mph}$$

2. Initial Velocity of the ball in the y direction

$$V_{b_{y0}} = V_{\text{after}} \sin(\alpha) = 3.51 \text{ m/s} (.559) = 1.96 \text{ m/s} = 4.38 \text{ mph}$$

3. Find position of y using the following equation

$$y = V_{b_{y0}} t + \frac{1}{2} a t^2$$

$$y = 1.96 \text{ m/s} (t) + \frac{1}{2} (-9.8 \text{ m/s}^2) (t^2)$$

$$\text{for } t = .01 \text{ s } y = .02 \text{ m} = .79 \text{ in}$$

$$\text{for } t = .39 \text{ s } y = .019 \text{ m} = .75 \text{ in}$$

4. The acceleration of the ball in the y direction at any
 time is $V_{by}^2 = (V_{b_{y0}})^2 + a y$

to get the maximum height, $V_{by}^2 = 0$

$$y = (-V_{b_{y0}}^2) / a = (-1.96 \text{ m/s})^2 / (-9.8 \text{ m/s}^2) = .39 \text{ m} = 15.35 \text{ in}$$

5 Horizontal direction is

$$V_{bx0} = V_{b\text{after}} * \cos(\alpha) = 3.51 \text{ m/s} (.829) = 2.91 \text{ m/s} = 6.51 \text{ mph}$$

6. Since gravity does not act in this direction, the following equation will give us the position of x

$$x = V_{bx0} * t = 2.91 \text{ m/s} (t)$$

$$\text{for } t = .01 \text{ s} \quad x = .03 \text{ m} = 1.18 \text{ in}$$

$$\text{for } t = .39 \text{ s} \quad x = 1.14 \text{ m} = 44.88 \text{ in}$$

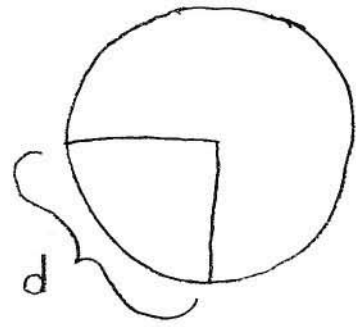
6 Iron

6 iron angle is 31°

Club length is $37.25 \text{ in} = .95 \text{ m}$

Mass of the ball $M_b = 46 \text{ g}$

Mass of the club head $= 280 \text{ g}$



Circumference $= 2\pi r$

Distance

$$d = \frac{1}{4}(2\pi r) = \frac{1}{4}(2)(3.14)(37.25 \text{ in}) = 58.48 \text{ in} = 1.49 \text{ m}$$

Time

$$t = .55 \text{ s}$$

Acceleration of gravity

$$a = 9.8 \text{ m/s}^2$$

Time ball is in flight from initial to when to landing t varying from .015 to .38 s

At maximum time of .38 s the ball traveled in x direction $= 50 \text{ in} = 1.27 \text{ m}$

Calculations: Impact velocity $V_i = d/t = 1.49 \text{ m} / .55 \text{ s} = 2.71 \text{ m/s} = 6 \text{ mph}$

Partial V_i is the portion of V_i that propels the ball

$$V_{i*} = V_i (\cos 31^\circ) = 2.71 \text{ m/s} (.857) = 2.32 \text{ m/s} = 5.19 \text{ mph}$$

1. Velocity of the ball after impact

$$V_{\text{batter}} = (M_c V_{i*} (1+e)) / (M_c + M_b)$$

$$V_{\text{batter}} = [280 \text{ g} (2.32 \text{ m/s}) (1+0.85)] / (280 \text{ g} + 46 \text{ g}) = 3.64 \text{ m/s} = 8.25 \text{ mph}$$

2. Initial Velocity of the ball in the y direction

$$V_{b y 0} = V_{\text{batter}} \sin(\alpha) = 3.64 \text{ m/s} (.515) = 1.90 \text{ m/s} = 4.25 \text{ mph}$$

3. Find position of y using the following equation

$$y = V_{b y 0} t + \frac{1}{2} a t^2$$

$$y = 1.90 \text{ m/s} (t) + \frac{1}{2} (-9.8 \text{ m/s}^2) (t^2)$$

$$\text{for } t = .015 \quad y = .02 \text{ m} = .79 \text{ in}$$

$$\text{for } t = .38 \text{ s} \quad y = .014 \text{ m} = .55 \text{ in}$$

4. The acceleration of the ball in the y direction at any time is $V_{by}^2 = (V_{by0})^2 + a * y$ to get the maximum height, $V_{by}^2 = 0$ $y = (-V_{by0}^2) / a = (-1.90 \text{ m/s})^2 / (-9.8 \text{ m/s}^2) = .37 \text{ m} = 14.56 \text{ in}$

5. Horizontal direction is $V_{bx0} = V_{b \text{ after}} * \cos(\alpha) = 3.64 \text{ m/s} (8.5)$
 $= 3.16 \text{ m/s} = 7.07 \text{ mph}$

6. Since gravity does not act in this direction, the following equations will give us the position of x

$$x = V_{bx0} * t = 3.16 \text{ m/s} (t)$$

$$\text{for } t = .015 \quad x = .03 \text{ m} = 1.18 \text{ in}$$

$$\text{for } t = .385 \quad x = 1.20 \text{ m} = 47.24 \text{ in}$$

5 Iron

Angle: 28° Club Length: $37.75 \text{ in} = .96 \text{ m}$
Mass of Ball (M_b): 46 g Mass of Club Head (M_c): 280 g

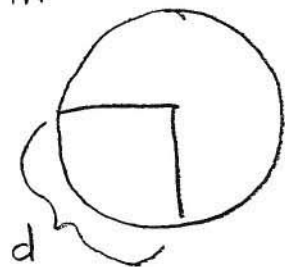
$$\text{Circumference} = 2\pi r$$

$$\text{Distance } (d) = \frac{1}{4} (2) (3.14) (37.75 \text{ in.}) = 59.27 \text{ in} = 1.51 \text{ m}$$

$$\text{Time } (t) = .55 \text{ s}$$

$$\text{Acceleration of Gravity } (a) = 9.8 \text{ m/s/s}$$

Time ball is in flight from initial launch to landing
 t varying from $.01 \text{ s}$ to $.35 \text{ s}$



At maximum time of $.35 \text{ s}$ the ball traveled in x direction $= 44 \text{ in}$
 $44 \text{ in} = 1.12 \text{ m}$

$$\text{Impact velocity } V_i = d/t = 1.51 \text{ m} / .55 \text{ s} = 2.75 \text{ m/s} = 6.15 \text{ mph}$$

Partial V_i is the portion of V_i that propels the ball

$$V_i^* = V_i (\cos 28^\circ) = 2.75 \text{ m/s} (.883) = 2.43 \text{ m/s} = 5.44 \text{ mph}$$

(1) Velocity of the ball after impact

$$V_{b \text{ after}} = (M_c V_i^* (1+e)) / (M_c + M_b)$$

$$V_{b \text{ after}} = [280 \text{ g} (2.43 \text{ m/s}) (1 + .85)] / (280 \text{ g} + 46 \text{ g}) = 3.86 \text{ m/s}$$

$$3.86 \text{ m/s} = 8.63 \text{ mph}$$

(2) Initial Velocity of the ball in the y direction

$$V_{b y_0} = V_{b \text{ after}}^* \sin(\alpha) = 3.86 \text{ m/s} (.469) = 1.81 \text{ m/s} = 4.05 \text{ mph}$$

(3) Find position of y using the following equation

$$y = V_{b y_0}^* t + \frac{1}{2} a^* t^2$$

$$y = 1.81 \text{ m/s } (t) + \frac{1}{2} (-9.8 \text{ m/s/s } (t^2))$$

$$\text{for } t = .01 \text{ s } y = .02 \text{ m} = .79 \text{ in}$$

$$\text{for } t = .35 \text{ s } y = .033 \text{ m} = 1.30 \text{ in}$$

(4) The acceleration of the ball in the y direction at any time

$$V_{b y}^2 = (V_{b y_0})^2 + a^* y$$

to get maximum height, $V_{b y}^2 = 0$

$$y = (-V_{b y_0}^2) / a = (-1.81 \text{ m/s})^2 / (-9.8 \text{ m/s/s}) = .33 \text{ m} = 12.99 \text{ in}$$

(5) Horizontal direction is

$$V_{b x_0} = V_{b \text{ after}}^* \cos(\alpha) = 3.86 \text{ m/s} (.883) = 3.41 \text{ m/s} = 7.63 \text{ mph}$$

(6) Since gravity does not act in this direction, the following equation will give us the position of x

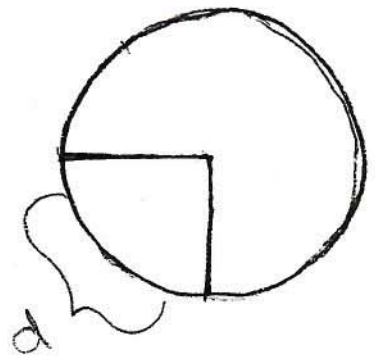
$$x = v_{bx0} * t = 3.41 \text{ m/s} (t)$$

$$\text{for } t = .01 \text{ s } x = .03 \text{ m} = 1.18 \text{ in}$$

$$\text{for } t = .35 \text{ s } x = 1.19 \text{ m} = 46.85 \text{ in}$$

4 Iron

4 iron angle is 25°
 Club length is $38.25 \text{ in} = .97 \text{ m}$
 Mass of the ball $M_b = 46 \text{ g}$
 Mass of the club head $M_c = 280 \text{ g}$



Circumference $= 2\pi r$

Distance

$$d = \frac{1}{4} (2\pi r) = \frac{1}{4} (2)(3.14)(38.25 \text{ in}) = 60.05 \text{ in} = 1.53 \text{ m}$$

Time

$$t = .55 \text{ s}$$

Acceleration of gravity

$$a = 9.8 \text{ m/s}^2$$

Time ball is in flight from initial launch to landing t varying
 from .01 s to .34 s

At maximum time of .34 s the ball traveled in x direction $= 53 \text{ in} = 1.35 \text{ m}$

Calculations

$$\text{Impact velocity } V_i = d/t = 1.53 \text{ m} / .55 \text{ s} = 2.78 \text{ m/s} = 6.22 \text{ mph}$$

Partial V_i is the portion of V_i that propels the ball

$$V_i^* = V_i (\cos 25^\circ) = 2.78 \text{ m/s} (.906) = 2.52 \text{ m/s} = 5.64 \text{ mph}$$

1) Velocity of the ball after impact

$$V_{\text{after}} = (M_c V_i^* (1+e)) / (M_c + M_b)$$

$$V_{\text{after}} = [280 \text{ g} (2.52 \text{ m/s}) (1+0.85)] / (280 \text{ g} + 46 \text{ g}) = 4.00 \text{ m/s} = 8.95 \text{ mph}$$

(2) Initial velocity of the ball in the y direction

$$V_{by0} = V_{\text{after}} \sin(\alpha) = 4.00 \text{ m/s} (.422) = 1.69 \text{ m/s} = 3.78 \text{ mph}$$

(3) Find position of y using the following equation

$$y = V_{by0} t + \frac{1}{2} a t^2$$

$$y = 1.69 \text{ m/s} (t) + \frac{1}{2} (-9.8 \text{ m/s}^2) (t^2)$$

$$\text{for } t = .01 \text{ s } y = .002 \text{ m} = .79 \text{ in}$$

$$\text{for } t = .34 \text{ s } y = .009 \text{ m} = .35 \text{ in}$$

(4) The acceleration of the ball in the y direction at any time is

$$V_{by}^2 = (V_{by0})^2 + a y$$

to get the maximum height, $V_{by}^2 = 0$

$$y = (-V_{by0}^2) / a = (-1.69 \text{ m/s})^2 / (-9.8 \text{ m/s}^2) = .29 \text{ m} = 11.42 \text{ in.}$$

(5) Horizontal direction is

$$V_{bx0} = V_{\text{after}} \cos(\alpha) = 4.00 \text{ m/s} (.906) = 3.62 \text{ m/s} = 8.10 \text{ mph}$$

(6) Since gravity does not act in this direction, the following equation will give us the position of x

$$x = V_{bx0} t = 3.62 \text{ m/s}$$

$$\text{for } t = .01 \text{ s } x = .04 \text{ m} = 1.57 \text{ in} \quad \text{for } t = .34 \text{ s } x = 1.23 \text{ m} = 48.43 \text{ in}$$

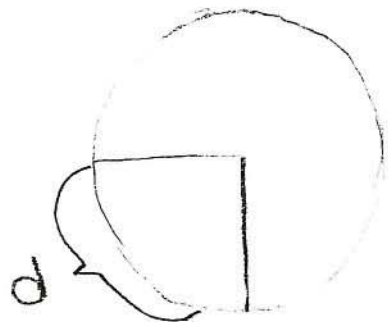
3 Iron

Angle: 22°

Club Length: $38.75 \text{ in} = .98 \text{ m}$

Mass of ball (m_B) = 46 g

Mass of the club head (m_C) = 280 g



Circumference = $2\pi r$

Distance

$$d = \frac{1}{4}(2\pi r) = \frac{1}{4}(2)(3.14)(38.75 \text{ in}) = 60.84 \text{ in} = 1.55 \text{ m}$$

Time

$$t = .55 \text{ s}$$

Acceleration of gravity

$$a = 9.8 \text{ m/s}^2$$

Time ball is in flight from initial launch to landing

t varying from $.01 \text{ s}$ to $.29 \text{ s}$

At maximum time of $.29 \text{ s}$ the ball traveled in x

$$\text{direction} = 38 \text{ in} = .97 \text{ m}$$

Calculations

$$\text{Impact velocity } V_i = d/t = 1.55 \text{ m} / .55 \text{ s} = 2.73 \text{ m/s} = 6.11 \text{ mph}$$

Partial V_i is the proportion of V_i that propels the ball

$$V_i^* = V_i (\cos 22^\circ) = 2.73 \text{ m/s} (.927) = 2.53 \text{ m/s} = 5.66 \text{ mph}$$

(1) Velocity of the ball after impact

$$V_{\text{After}} = (m_C V_i^* (1 + e)) / (m_C + m_B)$$

$$V_{\text{After}} = [280 \text{ g} (2.53 \text{ m/s}) (1 + 0.85)] / (280 \text{ g} + 46 \text{ g}) = 4.02 \text{ m/s} = 8.99 \text{ mph}$$

(2) Initial Velocity of the ball in the y direction

$$V_{by0} = V_{\text{After}} \sin(\alpha) = 4.02 \text{ m/s} (.375) = 1.51 \text{ m/s} = 3.38 \text{ mph}$$

(3) Find position of y using the following equation

$$y = V_{by0} t + \frac{1}{2} a t^2$$

$$y = 1.51 \text{ m/s} (t) + \frac{1}{2} (-9.8 \text{ m/s}^2) (t^2)$$

$$\text{for } t = .01 \text{ s} \quad y = .02 \text{ m} = .79 \text{ in}$$

$$\text{for } t = .29 \text{ s} \quad y = .626 \text{ m} = 24.69 \text{ in}$$

4) The acceleration of the ball in the y direction at any time is:

$$V_{by}^2 = (V_{by0})^2 + a * y$$

to get the maximum height, $V_{by}^2 = 0$

$$y = (-V_{by0}^2) / a = (-1.51 \text{ m/s})^2 / (-9.8 \text{ m/s}^2) = .23 \text{ m} = 9.06 \text{ in}$$

(5) Horizontal direction is

$$V_{bx0} = V_{b\text{after}} * \cos(\alpha) = 4.02 \text{ m/s} (.927) = 3.73 \text{ m/s} = 8.34 \text{ mph}$$

(6) Since gravity does not act in this direction, the following equation will give us the position of x

$$x = V_{bx0} * t = 3.73 \text{ m/s} (t)$$

$$\text{for } t = .01 \text{ s } x = .04 \text{ m} = 1.57 \text{ in}$$

$$\text{for } t = .29 \text{ s } x = 1.08 \text{ m} = 42.52 \text{ in}$$